### **NASA GRC Fatigue Crack Initiation Life Prediction Models**

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Metal fatigue has plagued structural components for centuries, and it remains a critical durability issue in today's aerospace hardware. This is true despite vastly improved and advanced materials, increased mechanistic understanding, and development of accurate structural analysis and advanced fatigue life prediction tools. Each advance is quickly taken advantage of to produce safer, more reliable, more cost effective, and better performing products. In other words, as the envelop is expanded, components are then designed to operate just as close to the newly expanded envelop as they were to the initial one. The problem is perennial.

The economic importance of addressing structural durability issues early in the design process is emphasized. Tradeoffs with performance, cost, and legislated restrictions are pointed out. Several aspects of structural durability of advanced systems, advanced materials and advanced fatigue life prediction methods are presented. Specific items include the basic elements of durability analysis, conventional designs, barriers to be overcome for advanced systems, high-temperature life prediction for both creep-fatigue and thermomechanical fatigue, mean stress effects, multiaxial stress-strain states, and cumulative fatigue damage accumulation assessment.

## NASA-GRC Fatigue Crack Initiation Life Prediction Models

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### NASA-GRC Fatigue Crack Initiation Life Prediction Models

#### Abstract

Metal fatigue has plagued structural components for centuries, and it remains a critical durability issue in today's acrospace hardware. This is true despite (a) the development of vastly improved and advanced materials. (b) increased mechanistic understanding, and (c) development of accurate structural analysis and advanced fatigue life prediction tools. Each advance is quickly taken advantage of to produce safer, more reliable, more cost effective, and better performing products. In other words, as the envelop of capability expands, components are designed to operate just as close, or even closer, to the newly expanded limits as they did to the initial ones. The problem is perennial.

The economic importance of addressing structural durability issues early in the design process is emphasized. Durability tradeoffs with performance, cost, and legislated restrictions are pointed out. Several unique aspects of structural durability of advanced systems, advanced materials and advanced fatigue life prediction methods are presented. Specific items to be discussed include the basic elements of durability analysis, conventional designs, barriers to be overcome for advanced systems, high-temperature life prediction for both creep-fatigue and thermomechanical fatigue, mean stress effects, multiaxial stress-strain states, and cumulative fatigue damage accumulation assessment. While not classified as being truly mechanistic models with a micromechanistic basis, they do contain aspects traceable to macroscopic, cause-and-effect phenomena. In their present form, the models are deterministic. Some examples of their application is presented. The models are awaiting efforts to be recast into probabilistic interpretation.

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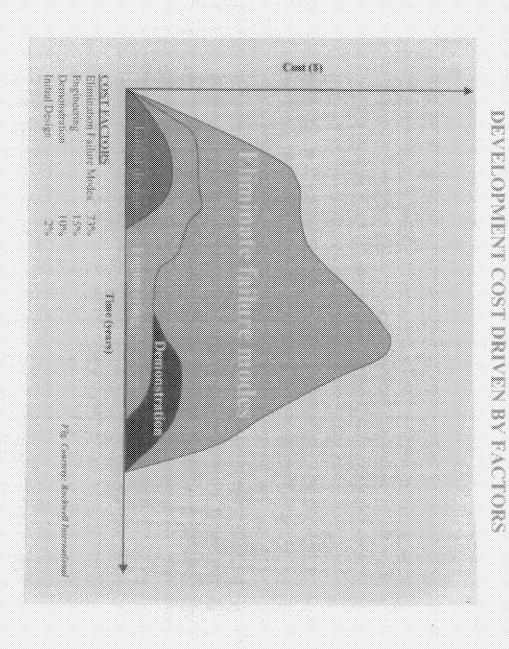
### OUTLINE

#### 0 - SETTING THE STAGE

- Cost of Elimination of Failure Modes
- Structural Durability Vs. Performance Vs. Cost
  - Durability, the poor step child
  - Life prediction a perennial problem (local vs. global)
  - Prediction vs. Verification dilemma

#### 0 - GLENN DURABILITY LIFING MODELS

- Specific Material Models (for example, Oxidation, Coatings, Brittle Materials, etc.)
- Damage Mechanics Models
- Fatigue Crack Growth Models
- Multi-Factor Approach
- Fatigue Crack Initiation/Early Growth Models
  - -- Estimating Fatigue Curves (LCF & HCF)
  - Modeling Effects of Variables
    - Mean stresses
    - Notches
    - Multiaxiality
    - Cumulative Fatigue Damage
    - Creep-Fatigue
    - Thermomechanical Fatigue
  - Probabilistic Assessment of Non-Linear Effects



## **Primary Trade-off Troika Drivers**

PERFORMANCE

DURABILITY =>

COST

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# Overriding Requirements Legislated / Public Outcry



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## **Elements of Durability Analyses**

- 0 Mission and Environmental Loading Analysis
- 0 Global Structural Response Analysis
- 0 Local Stress-Strain-Temp-Time Material Response Analysis
- 0 Durability Failure Modes Analysis
- 0 Damage Accumulation and Life Prediction Analysis
- 0 Coupon & Hardware Testing for Model Calib./Valid./Verif.
- 0 Mfg Quality Analysis and Non-Destructive Evaluation (NDE)

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### PEDESTRIAN DESIGNS

- 0 Previous design experience
- 0 Directly applicable rules of thumb
- 0 Previous mission experience on similar hardware
- 0 Extensive material property data bases
- 0 Knowledge of all potential failure modes
- 0 Knowledge of synergistic durability interactions
- 0 Affordable 'build-em' and bust-em' prototypes

- 0 Lack of previous direct experience/rules of thumb
- 0 Limited material property data bases
  - -- long-term data bases unachievable in timely manner
- 0 Ignorance of failure modes / synergistic interactions
- 0 Low fidelity of damage accumulation/life models
- 0 Prototypes too expensive to test or lead times too long

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- 0 Accept up-front costs of designed-in durability
- 0 Require critical minimum data bases
  - Early initiation of long-term testing
- 0 Seek out failure modes & any synergism
- 0 Capture the "physics" of damage accumulation
- 0 Analytically model damage/life prediction
- 0 Maximize durability information from each test
  - Fewer tests, however, decrease assessment of probabilities of failure
- 0 Continuously update analytic models
- 0 Take advantage of probabilistic analyses where possible

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### Description

Estimates Fatigue Resistance of Materials (Extensive use, e.g. Rocketdyne - SSME design)

- Tensile Ductility & Tensile Strength

- Cryogenic, Ambient, High Temperatures (10% Rule)

Predicts Cyclic Life of Components Below Creep Regime

- Multiaxiality via Triaxiality Factor

- Mean Stress Correction

Predicts Cyclic Life of Notched Components

- Cyclic Stress-Strain Neuber Notch Analysis

Predicts Cumulative Damage Life of Components

- Mission Loading History Analyzed

Predicts Crack Nucleation & Early Growth

- Daniage Curve Approach & Double Linear Damage Rule for Mission

- Multiaxiality via Triaxiality Factor

- Mean Stress Correction

Predicts Cyclic Life of C-Section Components

- Multiaxiality via Triaxiality Factor

Predicts Cyclic Life of High-Temp Components (Adopted by FoMoCo - Manifold/Exhaust System Design)

Utilizes Raw Experimental Data;

- Total Strain Version of Strainrange Partitioning (SRP)

- Isothermal Creep-Fatigue Interaction Assessment

- Thermomechanical Fatigue Life Prediction

- Bitherms! Characterization

- Cyclic Stress-Strain-Time-Temperature Characterization

- Multiaxiality via Triaxiality Eactor

- Thermal Mean Stress Correction

### Non-Linear Cumulative Fatigue Damage Code-PDLDR

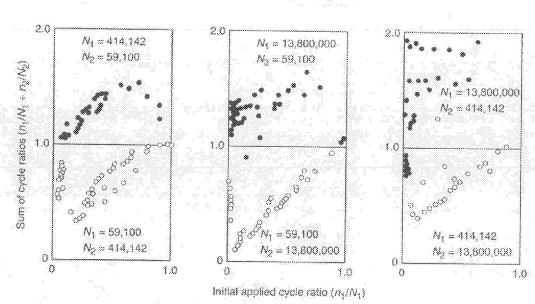
- 0 Why the Fuss?
  - Example of Material Behavior
- 0 Simple Models Developed
  - Require no more than Linear Damage Rule
- 0 Sample Calculations
  - Idealized Space Shuttle Component

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## Why the Fuss?

Classic Loading Order Effect in Two Load Level Cumulative Fatigue Damage Tests British Aluminum Alloy D.T.D. 683

- High- to low-cycle fatigue
- Low- to high-cycle fatigue



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### Generic Space Shuttle Component using Haynes 188 Alloy, 705 °C

(Double Linear Damage Rule Vs. Linear Damage Rule)

EXAMPLE APPLICATION - PDLDR

Loading Conditions Assumed:

0 - HCF Frequency 1000 Hz 0 - Mission Duration 500 sec

0 - HCF Life  $N_2 = 50,000,000$  Cycles to Failure 0 - LCF Life  $N_\perp = 500$  Cycles to Failure

Mission consists of  $n_1 = 1$  LCF Cycle  $n_2 = 500,000$  HCF Cycles

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# LINEAR DAMAGE RULE (LDR) PREDICTION OF NUMBER OF MISSIONS

$$2\left[\frac{n_1}{N_1} + \frac{n_2}{N_2}\right] = 10$$

$$\Sigma \left[ \frac{1}{500} + \frac{50,000}{50,000,000} \right] = \Sigma [0.002 + 0.010] = \Sigma 0.120 = 10$$

### 83 Number of Missions by LDR

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# DOUBLE LINEAR DAMAGE RULE (DLDR) PREDICTION OF NUMBER OF MISSIONS

Two Linear Damage Rules Summed to 1.0, Sequentially, Where:

$$N_1 + N_{II} = N_1$$

$$N_1 = f(N_1, N_1/N_2)$$

$$N_{II} = N_1 - N_1$$

PHASE I ("Initiation") =  $N_i$ :

$$\mathbb{E}\left[\frac{n_1}{N_{13}} + \frac{n_2}{N_{12}}\right] = 1.0$$

Then,

PHASE II ("Propagation") =  $N_{II}$ :

$$\Sigma \left[ \frac{n_1}{N_{H,1}} + \frac{n_2}{N_{H,2}} \right] = 1.0$$

Failure Occurs once Phase II reaches 1.0

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### Based on DLDR for Haynes 188 at 705 °C:

$$N_{I,1} = 10$$
  $N_{I,2} = 48,200,000$   $N_{II,1} = 490$   $N_{II,2} = 1,800,000$   $N_1 = 500$   $N_2 = 50,000,000$ 

 $\underline{PHASE\ I\ ("Initiation")} = N_i$ 

$$\Sigma \left[ \frac{n_1}{N_{I,1}} + \frac{n_2}{N_{I,2}} \right] = 1.0 \implies \Sigma \left[ \frac{1}{10} + \frac{500,000}{48,200,000} \right] = \Sigma [0.1 + 0.013 = 0.113] = 1.0$$

1 0.113 = 8.8 Missions to "Initiate"

Then,

PHASE II ("Propagation") =  $N_n$ :

$$\Sigma \left[ \frac{n_1}{N_{H,1}} + \frac{n_2}{N_{H,2}} \right] = 1.0 = \Sigma \left[ \frac{1}{490} + \frac{500,000}{1,800,000} \right] = \Sigma [0.002 + 0.278 = 0.28 = 1.0] = 1.0$$

 $8.8 \pm 3.6 = 12.4$ 

## $\approx 12$ Missions to Failure by DLDR vs. 83 Missions by LDR

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## EFFECT ON MISSION LIFE OF IMPROVING FATIGUE RESISTANCE

	Improvement	LDR (% increase) DLDR (% increase)	
645	Baseline Fatigue Curve	83 ()	12 ()
	Increase LCF by X2	91 (10%)	23 ( 90%)
	Increase HCF by X10	333 (300%)	25 (100%)
	Increase HCF by X100	476 (475%)	97 (700%)
	Increase LCF by X2		
	& HCF by X10	500 (500%)	37 (200%)

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## PSRPLIFE

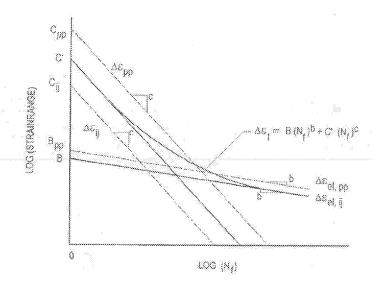
## EXAMPLE APPLICATIONS

- 0 StrainRange Partitioning (SRP)
  - Compared to Linear Time- and Cycle Life Fraction Rule
- 0 Schematic of Total Strain Version of StrainRange Partitioning (TS-SRP)
  - 0 Isothermal Total Strain Version of StrainRange Partitioning (TS-SRP)
    - Applied to Inconel 718 at 650 °C
  - 0 Thermomechanical Fatigue Version of TS-SRP
    - Applied to Haynes 188 & B-1900
    - Applied to Automotive Exhaust System Alloy (Ferritic 409 SS)

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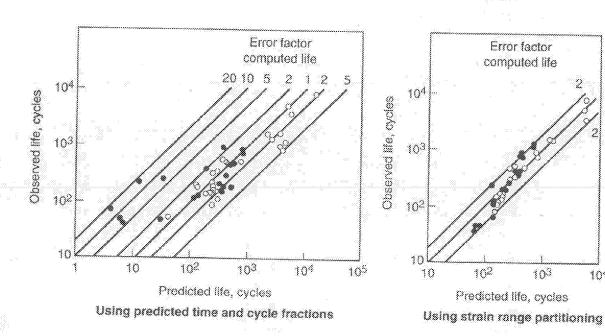
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# Schematic of Total Strain Version of StrainRange Partitioning (TS-SRP)



Prediction Capability Compared to Linear Time- and Cycle Life Fraction Rule

Creep-Fatigue Data for Incoloy 800 & 304 SS



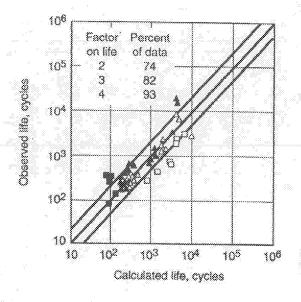
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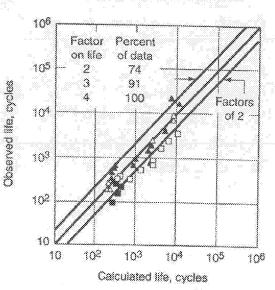
Isothermal Total Strain Version of StrainRange Partitioning (TS-SRP)

Predictability of Creep-Fatigue Data for Inconel 718 at 650 °C

Inelastic SRP



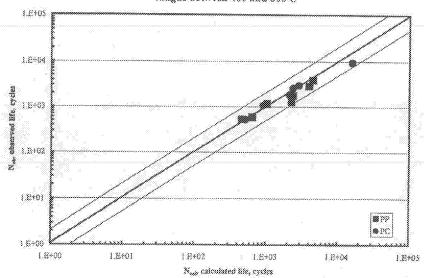
Total Strain Version



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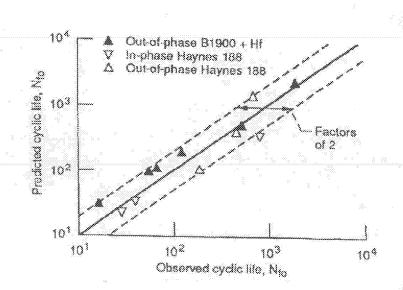
Thermomechanical Fatigue Version of SRP (TMF-SRP) Applied to Automotive Exhaust System Alloy (Ferritic 409 SS)

Correlation of calculated and observed fives of bithermal out-of-phase fatigue between 400 and 800  $\rm C$ 



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Thermomechanical Fatigue Version of SRP (TMF-SRP)
Applied to Haynes 188 & B-1900



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